## BUEC 333 QUIZ

Consider the following regression output from EViews, noting that wages give total annual earnings from wages and salaries, agegrp is 5-year age groups, where agegrp $=9$ is $25-29$ years old, hdgree indicates highest degree of schooling in 13 levels, sex=1 for women, citizen $=1$ for persons who are Canadian-by-birth, vismin indicates visible minority group membership, where values 1-12 are visible minority groups, and aboid indicates Aboriginal identity (including registry) for values 1-5.
Note that the regression output was generated by
QUICK--->EQUATION:
equation specification, using @expand:

```
log(wages) c @expand(agegrp, @dropfirst) @expand(hdgree, @dropfirst)
(vismin<13) (aboid<6) sex=1
```

sample:
156529 if agegrp>8 and agegrp<17 and wages>100 and citizen=1
Dependent Variable: LOG(WAGES)
Method: Least Squares
Date: 11/06/10 Time: 19:25
Sample: 156529 IF AGEGRP>8 AND AGEGRP<17 AND
WAGES>100
AND CITIZEN=1
Included observations: 13236

| Variable | Coefficient | Std. Error | t-Statistic | Prob. |
| :---: | ---: | ---: | ---: | ---: |
| C | 9.833821 | 0.038375 | 256.2582 | 0.0000 |
| VISMIN $<13$ | 0.020050 | 0.028715 | 0.698230 | 0.4850 |
| ABOID<6 | -0.212863 | 0.048369 | -4.400816 | 0.0000 |
| SEX=1 | -0.422557 | 0.016885 | -25.02616 | 0.0000 |
| AGEGRP $=10$ | 0.307883 | 0.030343 | 10.14672 | 0.0000 |
| AGEGRP=11 | 0.417287 | 0.030683 | 13.60013 | 0.0000 |
| AGEGRP=12 | 0.580113 | 0.030735 | 18.87470 | 0.0000 |
| AGEGRP=13 | 0.636205 | 0.030626 | 20.77356 | 0.0000 |
| AGEGRP $=14$ | 0.618184 | 0.032097 | 19.25971 | 0.0000 |
| AGEGRP=15 | 0.487574 | 0.034508 | 14.12919 | 0.0000 |
| AGEGRP=16 | 0.130724 | 0.042995 | 3.040436 | 0.0024 |
| HDGREE=2 | 0.283840 | 0.035274 | 8.046731 | 0.0000 |
| HDGREE=3 | 0.239772 | 0.046314 | 5.177108 | 0.0000 |
| HDGREE=4 | 0.415034 | 0.050108 | 8.282826 | 0.0000 |
| HDGREE=5 | 0.262411 | 0.048125 | 5.452640 | 0.0000 |
| HDGREE=6 | 0.388865 | 0.039400 | 9.869772 | 0.0000 |
| HDGREE=7 | 0.495839 | 0.047258 | 10.49211 | 0.0000 |
| HDGREE=8 | 0.439606 | 0.047437 | 9.267055 | 0.0000 |
| HDGREE=9 | 0.622720 | 0.037117 | 16.77728 | 0.0000 |
| HDGREE=10 | 0.586505 | 0.058468 | 10.03122 | 0.0000 |
| HDGREE=11 | 1.021631 | 0.112163 | 9.108484 | 0.0000 |
| HDGREE=12 | 0.760526 | 0.047171 | 16.12283 | 0.0000 |
| HDGREE=13 | 1.064670 | 0.100071 | 10.63910 | 0.0000 |
| HDGREE=88 | 0.261332 | 0.247468 | 1.056025 | 0.2910 |
| R-squared | 0.126205 | Mean dependent var | 10.43770 |  |
| Adjusted R-squared | 0.124684 | S.D. dependent var | 1.015558 |  |
| S.E. of regression | 0.950139 | Akaike info criterion | 2.737395 |  |
| Sum squared resid | 11927.32 | Schwarz criterion | 2.750977 |  |
| Log likelihood | -18092.08 | Hannan-Quinn criter. | 2.741929 |  |
| F-statistic | 82.96733 | Durbin-Watson stat | 2.124936 |  |
| Prob(F-statistic) | 0.000000 |  |  |  |

1) [4 points] Hypothesis Tests (provide reasoning or mathematical steps for all questions). You may assume that the $t$ distribution with the large a sample size is equal to the standard normal distribution.
a) $A G E G R P=12$ indicates a person aged 40-44. $A G E G R P=13$ indicates a person aged 45-49. Given these estimates, how much more does woman aged 48 earn than a woman aged 42? What about the same comparison for a man?
i) $0.636205-0.580113=0.056$, or about $5.6 \%$ more. ( 0.5 pt ) Same for a man, $\mathrm{b} / \mathrm{c}$ the female dummy cancels out. ( 0.5 pt )
b) Test the hypothesis that visible minority workers earn the same as white workers with the same age and education. Test the hypothesis that Aboriginal workers earn the same as white workers.
i) test stat=coef/std err=0.698230, which is less than the 10\% 2-sided crit (or whichever) for the $z$, so we don't reject the hyp that they earn the same ( 0.5 pt )
ii) test stat=coef/std err=-4.400816, which is bigger in absolute value than the 10\% 2-sided crit (or whichever) for the $z$, so we reject the hyp that Aboriginals earn the same as white workers. ( 0.5 pt )
c) Test the hypothesis that white workers have a log-earnings premium in comparison with Aboriginal workers that is larger than 10 per cent.
i) 0.5 pt each for noticing that it is one-sided and noticing that you check the distance of the coef from -0.1 . test stat is $-0.212863-(-0.1) / 0.048369=$ about -2.4 , which is bigger in absolute value than any alpha 1 -sided crit. So, we reject that hypothesis that is it as small as -10 per cent.
d) The t -statistic for the constant term ( C ) is very large. Why is it so large?
i) it tests whether the constant term is zero. the constant gives you the conditional expectation of log-earnings for a person whose other covariates equal 0 , that is a man aged 25-29 with just high school education. If the constant was zero, their expected log-earnings would be zero, corresponding to earnings of $\$ 1$. Thus, it is an uninteresting hypothesis.
2) [4 points] Other Topics (provide reasoning or mathematical steps for all questions)
a) R-squared is 0.126205 . Does that mean that 87.3 per cent of the variation of log-earnings is unexplained? Does that mean that the regression is not informative? Does that mean that we should disregard that results of the tests above?
i) yes, it means that 87.3 per cent of the variation of log-earnings is unexplained by the regressors, but that doesn't mean the regression doesn't capture how the conditional mean of log-earnings varies with the regressors, indeed it does. So, there is no need to disregard the results.
b) Does the inclusion of both (vismin<13) and (sex=1) induce multicollinearity? If so, how?
i) it does not, because visible minorities are just as likely to be women as are white people.
c) Suppose that earnings were correlated with field-of-study, with mathematical fields of study having higher earnings than nonmathematical fields of study. Suppose also that visible minorities are more likely to choose mathematical fields of study. Describe formally how this might lead to endogeneity. Describe how it would change your interpretation of the coefficient on (vismin<13).
i) the correlated missing regressor is field of study, and the endogeneity is equal to the coefficient on field of study multiplied by the covariance of field of study with vismin (they do not need to state that this is a partial covariance or mention FWL theorem). since both are nonzero, there is endogeneity. ( 0.5 pt )
ii) the coefficient on vismin (without field of study in the regression) captures the effect of vismin plus the load of visible minority's field of study on log-earnings.
d) Suppose that the data included a variable called age equal to the exact age in years for each respondent. In that case, would it have been a good idea to drop the age group variables and replace them simply with the one age variable? Why or why not?
i) the coefficients on age group suggest that the response to age is not linear: it is hump-shaped. therefore that strategy would induce specification error, which would bias the coefficients.
3) [2 points] Suppose that $Y_{i}=\beta_{0}+\beta_{1} X_{i}+u_{i}+v_{i} \quad$ and that $u_{i}$ and $v_{i}$ are 2 independently distributed random variables, each of which takes on the value -1 with $50 \%$ probability and the value 1 with $50 \%$ probability. Using the 6 classical assumptions, suppose that we regress $Y$ on $X$. Using the 6 classical assumptions, show whether or not the estimated OLS coefficients are unbiased. Using the 6 classical assumptions, show whether or not the estimated OLS coefficients are efficient.
a) yes, both unbiased and efficient.
b) unbiased: the sum of $u$ and $v$ is distributed $[-2,0,2]$ with probabilities $[0.25,0.50,0.25)$. The expectation of this is zero. This is true no matter what value $x$ takes on. Thus, $x$ is exogenous, because the covariance of $x$ and $u+v$ is zero. (1.5 pts)
c) efficient: given the pdf above, which doesn't vary with $x$ or with i, the errors are homoskedastic and not correlated across observations. ( 0.5 pt )

## Some probabilities for the standard normal distribution, $z$.

2 tailed probabilities: $\operatorname{Prob}[-1.65<z<1.65]=0.90, \operatorname{Prob}[-1.96<z<1.96]=0.95, \operatorname{Prob}[-2.56<z<2.56]=0.99$
1 tailed probabilities: $\operatorname{Prob}[z<1.28]=0.90, \operatorname{Prob}[z<1.65]=0.95$, $\operatorname{Prob}[z<2.33]=0.99$

## The 6 Classical Assumptions

1. The regression model is linear in the coefficients, correctly specified, and has an additive error term.
2. The error term has zero population mean: $E\left(\varepsilon_{i}\right)=0$.
3. All independent variables are uncorrelated with the error term: $\operatorname{Cov}\left(X_{i}, \varepsilon_{i}\right)=0$ for each independent variable $X_{i}$
4. Errors are uncorrelated across observations: $\operatorname{Cov}\left(\varepsilon_{i}, \varepsilon_{j}\right)=0$ for two observations $i$ and $j$ (no serial correlation).
5. The error term has constant variance: $\operatorname{Var}\left(\varepsilon_{i}\right)=\sigma^{2}$ for every $i$ (no heteroskedasticity).
6. No independent variable is a perfect linear function of any other independent variable (no perfect multicollinearity).

## Useful Formulae:

$\mu_{x}=E(X)=\sum_{i=1}^{k} p_{i} x_{i} \quad \operatorname{Var}(X)=E\left[\left(X-\mu_{X}\right)^{2}\right]=\sum_{i=1}^{k}\left(x_{i}-\mu_{X}\right)^{2} p_{i}$
$\operatorname{Cov}(X, Y)=\sum_{i=1}^{k} \sum_{j=1}^{m}\left(x_{j}-\mu_{X}\right)\left(y_{i}-\mu_{Y}\right) \operatorname{Pr}\left(X=x_{j}, Y=y_{i}\right)$

